Compiled: January 21, 2014

ECONOMETRIC THEORY EXERCICES 3 INFORMATION

Reference: Gouriéroux and Monfort (1995, Chapter 3)

- 1. Define the following notions:
 - (a) sufficient statistic;
 - (b) ancillary statistic;
 - (c) Fisher information;
 - (d) complete statistic.
- 2. Let Y_1, \ldots, Y_n be independent and identically distributed random variables with the same density $f(y; \theta)$. Show that the order statistics are sufficient for θ .
- 3. If the random variables Y_1, \ldots, Y_n are independent $N(0, \sigma^2)$, find a sufficient statistic for σ^2 .
- 4. State and demonstrate the factorization criterion for a sufficient statistic.
- 5. What are the sufficient statistics for an exponential model? Are these statistics minimal? Justify your answers.
- 6. Let $\ell(Y; \theta)$ be the likelihood function for the sample $Y = (Y_1, \dots, Y_n)'$. Show that

$$I(\theta) = E\left[-\frac{\partial^2 \log \ell(Y;\theta)}{\partial \theta \partial \theta'}\right].$$

- 7. When is parameter
 - (a) identifiable?
 - (b) locally identifiable?
- 8. When is a parametric model identifiable?

References

GOURIÉROUX, C., AND A. MONFORT (1995): Statistics and Econometric Models, Volumes One and Two. Cambridge University Press, Cambridge, U.K., Translated by Quang Vuong.